## REAL NUMBERS, POLYNOMIALS AND FRACTIONS TEST - 4º ESO



Exercise 1: (1 point) Rationalize:

a) 
$$\frac{6}{\sqrt{3}} = 2\sqrt{3}$$

b) 
$$\frac{14}{\sqrt[7]{2^3}} = 7\sqrt[7]{2^4}$$

c) 
$$\frac{\sqrt{5} + \sqrt{3}}{\sqrt{5} - \sqrt{3}} = 4 + \sqrt{15}$$

Exercise 2: (2.5 points) Work out, express as a single radical and simplify if possible:

a) 
$$2\sqrt{243} - 3\sqrt{1875} + \sqrt{192} = -49 \cdot \sqrt{3}$$
 (0.65)

b) 
$$\frac{\sqrt[3]{2^{-7} \cdot 3^5}}{\sqrt[5]{2^3 \cdot 3^{-7}}} = \frac{3^3}{2^2} \cdot \sqrt[15]{\frac{3}{2^{14}}}$$
 (0.75)

c) 
$$\sqrt[5]{x^{-4}} \cdot \sqrt{x^7} : \sqrt[3]{x^2} = x^2 \cdot \sqrt[30]{x}$$
 (0.7)

d) 
$$a^{-5/2} \cdot a^{3/4} : a^{-1/5} = \frac{1}{a} \cdot {}^{20}\sqrt{\frac{1}{a^{11}}}$$
 (0.4)

Exercise 3: (0.75 points) The flying time from Malaga to Bath is of two hours and forty minutes. Find the percentage error if we round it to two and three quarters hours  $E_p = 3.13\%$ 

**Exercise 4:** (1 point) Solve and factorize the equation  $x^6 + 12x^5 + 53x^4 + 102x^3 + 72x^2 = 0$ 

Roots: x = 0 double, x = -2, x = -3 double, x = -4

Factorization:  $x^2(x+2)(x+3)^2(x+4)$ 

Exercise 5: (0.75 points) Study the following unions and intersections of intervals:

a) 
$$[-2,1) \cup [-1,+\infty) = [-2,+\infty)$$

b) 
$$(-7,-1] \cap (-3,-2] = (-3,-2]$$

Exercise 6: (1 point) Work out:

a) 
$$3.68 \cdot 10^{-5} - 4.5 \cdot 10^{-4} + 1.39 \cdot 10^{-3} = 9.77 \cdot 10^{-4}$$

b) 
$$(8.37 \cdot 10^{-3}) \cdot (5.79 \cdot 10^{-7}) = 4.85 \cdot 10^{-9}$$

c) 
$$(3.82 \cdot 10^{-2})$$
:  $(8.91 \cdot 10^{-5}) = 4.29 \cdot 10^{2}$ 



Exercise 7: (3 points) Work out the value of the following expressions and simplify if possible:

a) 
$$\frac{x}{x^2 - 4x + 4} - \frac{x - 1}{x^2 - 4} + \frac{5}{2 - x} = \frac{-5x^2 + 5x + 18}{(x - 2)^2(x + 2)}$$
 (1.25)

b) 
$$\frac{10x^2 + 50x}{x^2 + 7x + 10} \cdot \frac{x^2 - 4}{5x^3 - 10x^2} = \frac{2}{x}$$
 (1)

c) 
$$\frac{x^2 + 10x + 25}{x^2 + 8x + 15}$$
:  $\frac{x^2 - 25}{x^2 - 9} = \frac{x - 3}{x - 5}$  (0.75)

